Weak PUF vs Strong PUF

The distinction is rooted in the security properties of their challenge-response pairs

One definition of a Strong PUF:

Even after giving an adversary access to the PUF instance for a prolonged period of time, it is still possible to come up with a challenge that with high probability, the adversary does not know the response

This implies that

• The PUF has a very large challenge space, otherwise the adversary can simply query the PUF with all challenges to learn its complete CRP behavior
• It is infeasible to build an accurate model of the PUF using only a subset of CRPs to ‘train’ the model, as a means of learning its complete CRP behavior

PUFs which do not meet these requirements are called Weak PUFs

In the limit, some PUFs have only a single challenge and are called physically obfuscated key or POK

We discussed the SRAM PUF earlier that has only one challenge
PUF Usage Scenarios

• **Identification**
  
The PUF can be used to generate a ’serial number’ to identify and/or track parts through manufacturing (the original proposed use by Keith Loftstrom in 1999!)

For manufacturing, *uniqueness* is the most important metric

  A *weak PUF* is sufficient for this type of *low security* application

Reliability is not a concern as long as

• Bit flip errors are infrequent, i.e., $\text{HD}_{\text{intra}}$ is relatively small, otherwise the probability of ’aliasing’ gets unacceptably large
• It is possible to use a ’fuzzy match’ criteria after the identifier is generated

• **Authentication**
  
The PUF is used to securely identify the chip in which it is embedded to an authority through corroborative evidence

As we will see when we discuss authentication scenarios, a *strong PUF* is best, particularly when the device is resource-constrained
PUF Usage Scenarios

Also, the **challenge-response** form of authentication implemented by strong PUFs is considered **strong**, in contrast to weak forms of authentication, e.g., passwords

Note that in contrast to encryption discussed below, the PUF inputs and outputs are **exposed** (to different degrees depending on the authentication scheme)

This makes the PUF more **accessible** (and vulnerable) to adversaries, and enables **model-building** attacks

There is a rapidly growing need for hardware-based authentication, e.g., in the supply chain, in the field (electronic voting machines) and for IoT devices

For the supply chain, the PUF is an important new security primitive that can address threats related to
- IC theft
- IC reuse
- Malicious substitution (hardware Trojans)
- Reverse engineering and cloning
PUF Usage Scenarios

The same is true for ’in the field’ authentication, particularly with IoT devices which are vulnerable to physical attacks and are resource-constrained.

All three statistical metrics, i.e., uniqueness, randomness and reliability, are important for authentication.

Some simple schemes relax the reliability metric as we will see.

Why use PUFs for authentication?

• They can eliminate the requirement for NVM, a real cost benefit for resource-constrained devices.
• They can potentially provide a very large number of CRPs, i.e., a much larger source of entropy when compared to an NVM.
• They are tamper-evident, making it more difficult for adversaries to physically probe the device to steal the secrets.
• They can be designed to never reveal their secrets, i.e., even the manufacturer does not have knowledge of the embedded secrets.
• They can be used to provide a stronger challenge-response form of authentication.
PUF Usage Scenarios

- **Encryption**
  The PUF is used to generate
  - A key for symmetric encryption algorithms
  - A random *nonce* that can be used to select a specific public-private key pair for asymmetric encryption

In typical encryption applications, the key is not revealed outside the chip and therefore, a *weak PUF* can be used (although a strong PUF is better here too)

The *inaccessability* of the PUF responses makes *model-building* impossible
However, recent work shows that power analysis attacks can be used to enable model-building, which argues in favor of using strong PUFs for encryption too

Unfortunately, in contrast to authentication schemes, **tolerance to bit flip errors is 0**
Even a difference of 1 bit in a 256-bit key completely wrecks communication between parties because of the avalanche effect
PUF Usage Scenarios

In summary

• All three applications require *uniqueness*

• Identification:
  
  PUF bitstrings must be large enough to suit the # of chips in the population

  \[ \text{HD}_{\text{intra}} \text{ can be } > 0 \text{ but bear in mind, this reduces the number of unique IDs that can be generated and used} \]

• Authentication: Add *randomness* as a critical metric

  Having a very large CRP space prevents adversaries from reading them all out and building a clone, and prevents them from succeeding at model-building

• Encryption: Adds both *randomness* and *reliability* as critical metrics

  Having a large number of CRPs is **not necessary** in cases where only a single key (or small number of keys) need to be generated over lifetime of chip

  \[ \text{HD}_{\text{intra}} \text{ must be zero, which requires } \textbf{error correction} \text{ or } \textbf{error avoidance} \]
**PUF Implementations**

There are MANY PUF implementations that have been proposed

A rough characterization is as follows:

- **Delay-based PUFs:**
  - Delays along ’matched’ paths (Arbiter)
  - Ring Oscillator frequencies
  - Glitches produced along paths within a functional unit
  - Delays along glitch-free paths within a functional unit (HELP)

- **Bi-stable PUFs:**
  - SRAM
  - Butterfly, Buskeepers
  - FFs and Latches

- **Mixed-Signal PUFs:** (These require a specialized analog-to-digital converter: ADC)
  - Transistor threshold voltage/transconductance
  - Dynamic/leakage current
  - Resistance/Capacitance
A specialized structure implements **two paths**, each of which can be individually configured using a set of *challenge bits*

Each of the challenge bits controls a ‘Switch box’, that can be configured in either **pass mode** and **switch mode**

*Pass mode* connects the upper and lower path inputs to the corresponding upper and lower path outputs, while *switch mode* flips the connections

A stimulus, represented as a rising edge, *cause two edges to propagate* along the two paths configured by the challenge bits
The faster path controls the value stored in the Arbiter located on the right side of the figure.

If the propagating rising edge on the upper input to the Arbiter arrives first, the response bit output becomes a ‘0’, otherwise a ’1’.

The switch boxes are designed identically as a means of avoiding any type of systematic bias in the delays of the two paths.

Within-die process variations change the delay through the switch boxes, which makes each instance of the Arbiter PUF unique.
It is clear that the arbiter PUF has an exponential number of input challenges. In particular, $2^n$ with $n$ representing the number of switch boxes.

However, the total amount of entropy is relatively small.

For $n$ equal to 128, the total number of path segments that can vary individually from one instance to another is $4 \times 128 = 512$.

The exponential number of challenges simply combine the entropy in different ways. Although the Arbiter PUF is considered a strong PUF, researchers have ’broken’ it using model building many times.
Another important issue is *meta-stability*

What happens with the two edges *arrive simultaneously* at the inputs to the arbiter?

The metastable condition eventually resolves, but the response bit in this case is **not** stable

In other words, repeating the challenge will produce different responses

The number of challenges that produce *metastable* (noisy) bits increases when temperature and supply voltage are varied
Model Building

The number of individual sources of entropy in the Arbiter is only linear with $n$

Therefore, **dependencies must exist** among the $2^n$ challenges and response bits

For example, if it were possible for the adversary to learn the *individual path segment delays*, then the PUF is no longer needed to predict the responses

Modeling attacks leverage a simple **additive delay model** where the delay of the entire path is equal to the sum of the individual segment delays

By strategically selecting CRPs, *machine-learning* techniques can quickly determine the **relative delays** through each switch box

Machine-learning techniques include *artificial neural networks* (ANNs), *support-vector machines* (SVMs), *genetic algorithms* and *decision trees*

Goal is deduce the relationship of segment delays using as few CRPs as possible

A PUF is \((p_{\text{model}}, q_{\text{train}})\)-**modelable** if known modeling attacks exist which have a successful prediction rate of $p_{\text{model}}$ after training with $q_{\text{train}}$ CRPs
**Arbiter PUF Evolution**

Early examples in the literature on ASIC implementations show
- $HD_{\text{intra}}$ of 4.82% with a temperature range of 25°C to 67°C
- $HD_{\text{inter}}$ of 23%
- SVM-based machine learning attack produced ($p_{\text{model}} = 96.45\%, q_{\text{train}} = 5000$), which indicates the implementation is not secure

All subsequent work attempt to make model-building attacks more difficult by:
- Introducing **non-linearities**, i.e., *feed-forward* and *XOR-mixed* versions
- Obfuscating the challenges to the PUF and the responses from the PUF

**XOR-mixed version**

![Diagram of XOR-mixed version of arbiter PUF](image)

- Challenge bits: $C_n, C_{n-1}, \ldots, C_0$
- Response bit: $DQ$
Ring Oscillator PUF

The RO PUF is also a delay-based PUF but the configuration and measurement technique are different from the Arbiter PUF

- An odd number of inverters are connected in a ring, which causes an edge to circulate continuously
- The Arbiter is replaced by a counter

By enabling the RO for a fixed $\Delta t$, the frequency of the RO is reflected in the count, and is given by $\frac{\text{count}}{\Delta t}$

But since $\Delta t$ is constant for all RO testing, the digital count value can be used instead

Similar to the Arbiter PUF, a differential frequency post-processing scheme is typically used to compensate for temperature/supply voltage variations
Here, a pair of ROs are selected to drive 2 separate counters
TV variations change the frequencies of both ROs in a similar fashion, significantly improving the reliability of the RO PUF

The RO PUF is a weak PUF
Assuming any RO can be paired with any other, we have $n(n - 1)/2$ pairings

Remember, model-building is not applicable to weak PUFs because it is possible to read out all possible bitstrings when the number is limited to $n^2$
Ring Oscillator PUF

However, not all these pairing produce independent evaluations.

If RO A is faster than RO B, and B is faster than C, than A is faster than C.

Therefore, the third response bit is dependent on the previous 2 bits.

The true amount of entropy is a function of the number of possible ordering of $n$ frequencies, which is $n!$.

Assuming each ordering is IID, the max. number of independent comparisons is

$$\log(n!) = \sum_{i=2}^{n} \log_2(i)$$

From Maes text.
**Ring Oscillator PUF**

Lehmer-Gray encoding has been proposed to optimize entropy and nearly achieves the maximum $\log_2(n!)$ number of independent response bits.

The cost is increased processing complexity.

A low-overhead strategy for dealing with dependencies is to use each RO **in only one comparison**.

This strategy is not optimal, however, in utilizing the available entropy, reducing the number of generated response bits to $n/2$. 

From Maes text
Metal Resistance PUF

The metal PUF measures voltage drops across polysilicon wires, metal wires and vias as the source of entropy

Stimulus-Measure-Circuit (SMC)

An SMC cell from a larger array is selected using column and row select signals

Once selected, a Stimulus-Measure-Circuit (SMC) enables a shorting transistor (stimulus) which creates a voltage drop across the poly-metal-via stack

Two 'pass gates' are also enabled that allow voltages to be sensed and measured
Metal Resistance PUF

Voltages generated by an element in the SMC are digitized by a VDC.

**SMC array of 2048 elements**

Vin, VOUT, VDD, VSS

A 2048 element SMC array is 16 rows high and 8 rows wide.

- **Digitized thermometer code (TC)**
  - 128 stages
  - TC = 85

**Voltage-to-digital-converter (VDC)**

- **First edge**
  - latches

- **Second edge**
  - latches

- **Fixed width**


Layout of the PUF Engine, VDC and SMC array IP block
Metal Resistance PUF

Similar to the RO bit generation method, the algorithm used for the metal PUF creates TC differences (TCDs) by randomly selecting pairs of TCs from the distribution.

An error avoidance scheme is proposed that creates two thresholds around the mean of the TCD distribution.

TCDs around the mean are unstable and are not permitted to generate a bit in the bit-string/key.

The red and blue TCDs illustrate that TV-noise-related variations during regeneration are small enough to prevent bit flip errors.

Metal Resistance PUF

Statistical analysis of bitstrings generated from 7343 TCDs and 63 chips

**Uniqueness**

- Ideal Ave. HD: 3671.5 bits
- Actual Ave. HD: Mean: 3,666.8, Std. Dev.: 43.4

<table>
<thead>
<tr>
<th></th>
<th>Inter-chip</th>
<th>Intra-chip</th>
</tr>
</thead>
<tbody>
<tr>
<td>HD %</td>
<td>49.94%</td>
<td>4.01%</td>
</tr>
</tbody>
</table>

Gaussian curve fit

**Randomness**

- # of passing chips
- NIST test number

We developed a reliability-enhancing technique called XMR, which creates redundant copies of the bitstring

**Majority voting** is then used to ’correct’ bit-flip errors

Typical reliability standards target $1e^{-6}$ (1 in a million) to $1e^{-9}$ (1 in a billion)

3MR (TMR) and 5MR provide reliability in this range
**Hardware Embedded Delay PUF (HELP)**

HELP measures path delays in an on-chip functional unit, e.g., AES, and leverages random **within-die** variations in **propagation delay** as a source of entropy.

HELP can be described entirely in an HDL, and therefore can be implemented on FPGAs.

The functional unit (entropy source) is implemented using a specialized logic style that is **hazard-free**.

This ensures paths remain **stable**, and can be timed accurately, as TV conditions vary.

HELP is a **STRONG PUF** and is capable of generating a large # of random bitstrings.
Hardware Embedded Delay PUF (HELP)

HELP uses a launch-capture timing mechanism to obtain high-resolution path delay values for combinational logic paths.

Path delays can be measured using a clock strobing method.

Or using an alternative flash ADC method that also works well.

The fine phase shift feature within modern digital clock managers (DCMs) can be used to incrementally tune a capture clock, $Clk_2$, in a series of launch-capture tests.

The integer-based fine phase shift value is used as the digitized path delay.
HELP Experiments and Features

We implemented HELP on a Xilinx Zynq 7020 and tested 20 chips, with 25 copies of HELP implemented in different locations (but ’fixed’) on each of the chips.

The total number of paths in the AES functional unit is approx. 8 million (4 million rising paths and 4 million falling paths).

This large # is the first important characteristic that makes HELP a strong PUF.

Other features are related to its multi-dimensional CRP space which includes:

- Parameters including two LFSR seeds, \( \mu_{\text{ref}} \) and \( Rng_{\text{ref}} \), a Modulus and Margin
- The full set of two vector sequences, Path-Select masks and Distribution Effect
HELP Processing Steps

**STEP 1:** Apply a set of challenges to generate 2048 *rising* path delays (called PNR) and 2048 *falling* path delays (called PNF), with PN for PUFNumber.

Changes in TV conditions shift and scale the digitized path delays.

These digitized path delays are processed as a group, NOT individually as is true of all other PUFs, i.e., no bits are generated until all group processing is complete.
HELP Processing Steps

**STEP 2**: Create **unique pairing** of rising and falling path delays using two *11-bit* LFSRs, to create PN Differences or **PND**

*Shifting* and *scaling* of entire distribution is exacerbated, but TV variations are reduced (*partially compensated* for) in the individual PND b/c of common mode

LFSR seeds expand the response space of HELP and allow up to \( n^2 \) bits to be generated from \( n \) PNR and \( n \) PNF

As we will see later, a **Modulus** operation nearly eliminates the classical *dependencies* that exist when PN are reused
HELP Processing Steps
Illustration of one PNR and one PNF, collected across 12 TV corners (x-axis) and 500 chips-instances (y-axis)

Single PNR/PNF illustrate that shifting and scaling is significant, while PND in right plot show reduced *jig-saw* pattern

Goal is to have *flat horizontal* lines, i.e., all TV corners produce same PND

The data from the 25 instances from Chip_{20} are highlighted in red to illustrate performance similarities

The large spread along y-axis is largely due to *chip-to-chip* variations
HELP Processing Steps

It's clear that the difference operation is NOT able to remove all of the path delay variation introduced by TV-noise.

**STEP 3:** Apply TVCompensation (TVComp) to remove remaining TV-noise

\[ zval_i = \frac{(PND_i - \mu_{\text{chip}})}{\text{Rng}_{\text{chip}}} \]

\[ PND_c = zval_i \times \text{Rng}_{\text{ref}} + \mu_{\text{ref}} \]

The \( \mu_{\text{chip}} \) and \( \text{Rng}_{\text{chip}} \) are computed from a histogram distribution.

The \( \text{ref} \) values are *user-specified* parameters.

TVComp creates a histogram distribution of PND, and then scales and shifts the path delay distribution to a *reference* distribution.

The *reference* distribution values **expand** the response space of HELP in a similar fashion to the 2 LFSR seeds used to create the PND from the PNR and PNF.
HELP Processing Steps

TVComp ELIMINATES all chip-to-chip variations, but preserves within-die variations.

This fact is illustrated on the right with $PND_c$, which show the data from the 25 instances from Chip$_{20}$ now distributed across entire range of y-axis.

In contrast to the grouping of Chip$_{20}$ data on the left, which shows similar performance among the different instances, as expected b/c data is from same chip.
HELP Processing Steps

The \( \text{PND}_c \), although compensated for TV variations, still possess \textit{path length} bias.

Bias is dealt with in two ways, first by optionally applying an \textit{Offset} (for fine tuning) and then using a coarse-grained \textit{Modulus} operation.

**STEP 4:** Add server-computed \textbf{Offsets} (computed using enrollment data) and then apply a \textbf{Modulus} operation to remove path length bias.

Offsets are computed from the \textbf{median of the chip population} and are added to each \( \text{PND}_c \), which shifts pop. to a multiple of 10 and then a \textbf{Modulus} of 20 is applied.

The \( \text{PND}_c \) with offsets are called \( \text{PND}_{co} \) and the final values are called \( \text{modPND}_{co} \).
HELP Processing Steps

STEP 5: Bitstring generation uses a **Margin** parameter, that implements a *bit-flip avoidance* reliability-enhancing scheme.

We call this the **Single Helper Data** scheme b/c the Margin scheme is run only by the token during enrollment.

We also have a **Dual Helper Data** scheme that combines helper data generated by both the token and server.

We have a suite of reliability-enhancing schemes for stand-alone (no server) applications, e.g., key-encryption-key (**KEK**) mode.
HELP Statistical Results
Statistics using the Offset method

These statistical results indicate the bitstrings generated by HELP are of cryptographic quality.
### HELP Area Overhead

<table>
<thead>
<tr>
<th>HELP Module</th>
<th>MUX</th>
<th>Carry</th>
<th>LUTs</th>
<th>FFs</th>
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<tbody>
<tr>
<td>PUF: CollectPNs</td>
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<td>PUF: ComputeModulus</td>
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<tr>
<td>PUF: DataTransferOut</td>
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<td>10</td>
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<td>PUF: DualHelpBitGen</td>
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<td>PUF: EvalMod</td>
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<td><strong>2014</strong></td>
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</table>

Additional resources include 1 MMCM, a 16 KB BRAM and a 24-bit multiplier

Note that this implementation of HELP includes all four functions, including *token authentication, verifier authentication, session encryption* and KEK

Versions dedicated to one function would be smaller in size